Notes on the function gsw_dynamic_enthalpy_t_exact(SA,t,p)

Young (2010) has defined dynamic enthalpy h^{\dagger} to be the difference between enthalpy and potential enthalpy, that is, $h - h^0 = h - c_p^0 \Theta$. Hence dynamic enthalpy h^{\dagger} is also equal to the following pressure integral of specific volume for a seawater parcel which does not exchange heat or salt as its pressure is changed during the integration,

$$\hat{h}^{\dagger}(S_{\mathrm{A}},\Theta,p) = h(S_{\mathrm{A}},\Theta,p) - c_{p}^{0}\Theta = \int_{P_{0}}^{P} \hat{v}(S_{\mathrm{A}},\Theta,p') dP', \qquad (1)$$

The lower limit of the integration is $P_0 \equiv 101325$ Pa and the pressure integral is done with pressure in Pa (not dbar). Enthalpy and dynamic enthalpy have units of J kg⁻¹.

This function, **gsw_dynamic_enthalpy_t_exact**(SA,t,p), evaluates dynamic enthalpy h^{\dagger} in terms of the input variables Absolute Salinity S_A *in situ* temperature *t* and pressure *p*. This function uses the full TEOS-10 Gibbs function $g(S_A, t, p)$ of IOC *et al.* (2010), being the sum of the IAPWS-09 and IAPWS-08 Gibbs functions.

This function is essentially the following calls to two other GSW functions,

```
CT = gsw_CT_from_t(SA,t,p);
dynamic_enthalpy_t_exact = gsw_enthalpy_t_exact(SA,t,p) - cp0*CT;
```

References

- IAPWS, 2008: Release on the IAPWS Formulation 2008 for the Thermodynamic Properties of Seawater. The International Association for the Properties of Water and Steam. Berlin, Germany, September 2008, available from <u>www.iapws.org</u>. This Release is referred to in the text as **IAPWS-08**.
- IAPWS, 2009: Supplementary Release on a Computationally Efficient Thermodynamic Formulation for Liquid Water for Oceanographic Use. The International Association for the Properties of Water and Steam. Doorwerth, The Netherlands, September 2009, available from http://www.iapws.org. This Release is referred to in the text as IAPWS-09.
- IOC, SCOR and IAPSO, 2010: The international thermodynamic equation of seawater 2010: Calculation and use of thermodynamic properties. Intergovernmental Oceanographic Commission, Manuals and Guides No. 56, UNESCO (English), 196 pp. Available from http://www.TEOS-10.org
- Young, W. R., 2010: Dynamic enthalpy, Conservative Temperature, and the seawater Boussinesq approximation. *Journal of Physical Oceanography*, **40**, 394–400.