Notes on the function, gsw_CT_from_entropy(SA, entropy), which evaluates Conservative Temperature from specific entropy

This function, **gsw_CT_from_entropy**, finds Conservative Temperature for given values of Absolute Salinity and specific entropy, $\Theta = \Theta(S_A, \eta)$. The function amounts to the following simple calls to two other GSW functions,

```
pt = gsw_pt_from_entropy(SA,entropy);
CT = gsw_CT_from_pt(SA,pt);
```

Here follows appendix A.10 of the TEOS-10 Manual (IOC et al. (2010)).

A.10 Proof that $\theta = \theta(S_A, \eta)$ and $\Theta = \Theta(S_A, \theta)$

Consider changes occurring at the sea surface, (specifically at p = 0 dbar) where the temperature is the same as the potential temperature referenced to 0 dbar and the increment of pressure dp is zero. Regarding specific enthalpy h and chemical potential μ to be functions of entropy η (in place of temperature t), that is, considering the functional form of h and μ to be $h = \hat{h}(S_A, \eta, p)$ and $\mu = \hat{\mu}(S_A, \eta, p)$, it follows from the fundamental thermodynamic relation (Eqn. (A.7.1)) that

$$h_{\eta}(S_{\rm A},\eta,0) \,\mathrm{d}\eta + h_{S_{\rm A}}(S_{\rm A},\eta,0) \,\mathrm{d}S_{\rm A} = (T_0 + \theta) \,\mathrm{d}\eta + \mu(S_{\rm A},\eta,0) \,\mathrm{d}S_{\rm A}, \qquad (A.10.1)$$

which shows that specific entropy η is simply a function of Absolute Salinity S_A and potential temperature θ , that is $\eta = \eta(S_A, \theta)$, with no separate dependence on pressure. It follows that $\theta = \theta(S_A, \eta)$.

Similarly, from the definition of potential enthalpy and Conservative Temperature in Eqns. (3.2.1) and (3.3.1), at p = 0 dbar it can be seen that the fundamental thermodynamic relation (A.7.1) implies

$$c_p^0 d\Theta = (T_0 + \theta) d\eta + \tilde{\mu}(S_A, \theta, 0) dS_A.$$
(A.10.2)

This shows that Conservative Temperature is also simply a function of Absolute Salinity and potential temperature, $\Theta = \Theta(S_A, \theta)$, with no separate dependence on pressure. It then follows that Θ may also be expressed as a function of only S_A and η . It follows that Θ has the "potential" property.