# An uncertainty budget for the **BOUSSOLE** radiometry, as derived using a Monte Carlo Method

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# **ABSTRACT**

The BOUSSOLE buoy [1,2,3] provides a long-term time series of radiometric quantities optical properties in support of calibration and validation activities of satellite ocean colour missions and bio-optics research in oceanic waters. The buoy is in continuous operation since 2003 and provided system vicarious calibration (SVC) data for the European MERIS instrument on-board ENVISAT, and will continue doing so for the new Copernicus Sentinel 3 satellites series. Remote Sensing Reflectance is the main product used for SVC therefore in real need for robust uncertainty budget assessment.

# **METHODOLOGY**

The Monte Carlo Method (MCM) for uncertainty evaluation[2] is based on a model (a measurement equation as Eq 1.) that uses inputs (Eq 1. right hand side) with associated probability distribution functions (PDFs) that hold information about their uncertainties. Then the model is run a large number of times repeating the same calculation each time by randomly drawing input values from theirs PDFs. The result of the MCM is a PDF of the outcome value ( $R_{rs}$  in our case) that is crated from those repeated calculations.

The best estimate and uncertainty of the output value is then evaluated from this distribution.



Fig 1.  $E_s(442)$  for a single full point i.e. denominator in Eq. 1. SZA=24 and buoy tilt  $< 4^{\circ}$ . The blue line represents the calculated value, the histogram behind is the output form MCM and indicate red lines standard uncertainty a standard expressed as of the output deviation values.

$$R_{rs} = \frac{\overline{L_{u4}}f_{cal}f_{s}exp\left[z_{4}\left(\frac{-\ln(\overline{L_{u9}}f_{cal}f_{s}/\overline{L_{u4}}f_{cal}f_{s})}{z_{9}-z_{4}}\right)\right]f_{H}f_{\rho n}}{\overline{E_{s}}f_{cal}f_{cos}f_{tilt}f_{dir} + (1-f_{dir})\overline{E_{s}}f_{cal}}$$
 Eq. 1.

 $L_{u4}$ ,  $L_{u9}$ ,  $E_s$  are median values of 1 minute measurements of two OCR radiometers (upwelling) radiance at 4 m,  $L_{u4}$ , and 9 m,  $L_{u9}$ ) Satlantic 200 series and one OCI (surface irradiance,  $E_s$ ) with 7 VIS spectral bands. The  $f_i$  terms represent correction factors for:

- absolute radiometric calibration  $(f_{cal})$ , diffuser cosine response  $(f_{cos})$ ,
- shading  $(f_s)$ , buoy tilt  $(f_{tilt})$ ,  $z_4$  and  $z_9$  are the actual instruments depths corrected for buoy tilt,
- extrapolation to surface using *Hydrolight* simulation  $(f_H)$ , the constant for water-air interface and fraction of the direct to total solar irradiance  $(f_{dir})$ .

## **EQUATION COMPONENTS AND UNCERTAINTY ASSESSMENT**

RAW READ	AW READINGS								
Median	and	standard	deviation						
Quality Controlled (QC) readings for SV									
• One minute readings									

### **INSTRUMENT RELATED**

0

Derived from laboratory tests with uncertainties defined in the traditional way. Gaussian PDFs with standard

#### **ENVIRONMENTAL**

Come from ancillary buoy data e.g. the buoy tilt, actual depth and MC Shading modelling [3]. Uncertainties

#### MODELLING

Defined derived by theory from available models, uncertainty estimated from literature, or sensitivity



#### Solar zenith angle

**Fig 6.**  $E_s$  standard uncertainties. Series numbers correspond to spectral channels. Each point corresponds to the evaluation of the denominator of **Eq.1** with  $f_{cal}$ ,  $f_{cos}$ ,  $f_{tilt}$  and  $f_{dir}$  randomly selected through the MC process.is a result from MC simulation. The visible step at SZA 60° is due to the average factory uncertainty of cosine diffuser response. Further decrease in values at higher SZA is due to the decrease of the direct light fraction.

#### Standard uncertaintyn (k = 1)

**Fig 7.** Summary of all simulations on SVC data set for all channels, SZAs and qualified environmental conditions. The uncertainty value used as representative of the whole set is 2.1 % which corresponds to the highest density. Uncertainty values for each variable and wavelength are derived in a similar manner.

560	2.0	2.6	3.1	3.7	0.0000725
665	2.1	3.9	5.9	6.3	0.0000410
681	2.1	4.0	5.9	6.3	0.0000195

3.0

3.7

0.000155

**Table 1.** Preliminary uncertainty budget.



REFERENCES

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